



# Equivalent Circuit and Electrodynamics Characteristics of Waveguide-Based Nozzleless Cylinder-Type Microwave Plasma Source



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## INTRODUCTION

We present equivalent circuit of existing waveguide-based nozzleless cylinder-type microwave plasma source (MPS). The waveguide-based cylinder-type MPS was used to convert methane into hydrogen. This MPS operates at atmospheric pressure and frequency of 2.45 GHz. The discussed cylinder-type MPS is based on rectangular waveguide WR 430. Equivalent circuit presented in this paper cannot describe all electrical properties of the real MPS accurately, due to some structural elements, which electrical lumped equivalents are difficult to find or are unknown. We used Comsol Multiphysics software to calculate some of them. The plasma column plunges partially into cylinders (non-symmetrically) creating two lossy coaxial lines. The central "wire" of this lossy coaxial lines is plasma column. Plasma is strongly non-linear element of the circuit because plasma impedance  $Z_p$  depends on incident microwave power.

## FORMULAS

Transformation factors:

$$k_T = \frac{Y_0}{Y_{01}} \quad k_S = \frac{Y_{01}}{Y_0} = k_T^{-1}$$

Normalized movable plunger susceptance in output plane:

$$b_S = \frac{B_S}{Y_0} = ctg\left(\frac{2\pi}{\lambda_g} \cdot l_S\right) = t_S^{-1}$$

Plasma impedance:

$$Z_p = R_p + jX_p$$

Normalized input admittance:

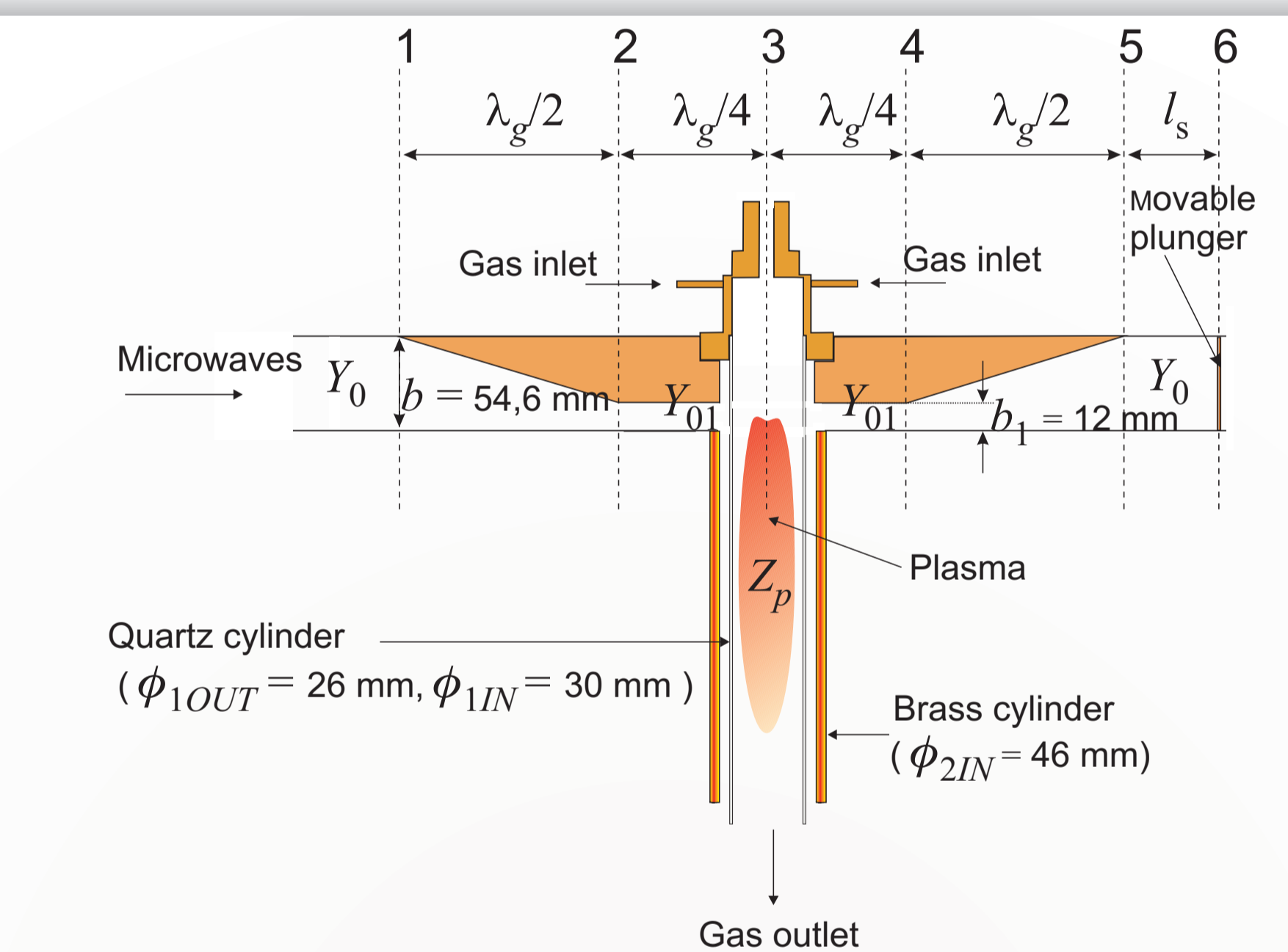
$$y_{in} = \frac{Y_1}{Y_0} = k_S \frac{Z_p^{-1} \cdot (Z_b Y_{01} - j b_S) + Y_{01}}{Z_a [Z_p^{-1} (Z_b Y_{01}^2 - j k_S Y_0 b_S) + Y_{01}^2] - j k_S Y_0 b_S}$$

Tuning characteristic:

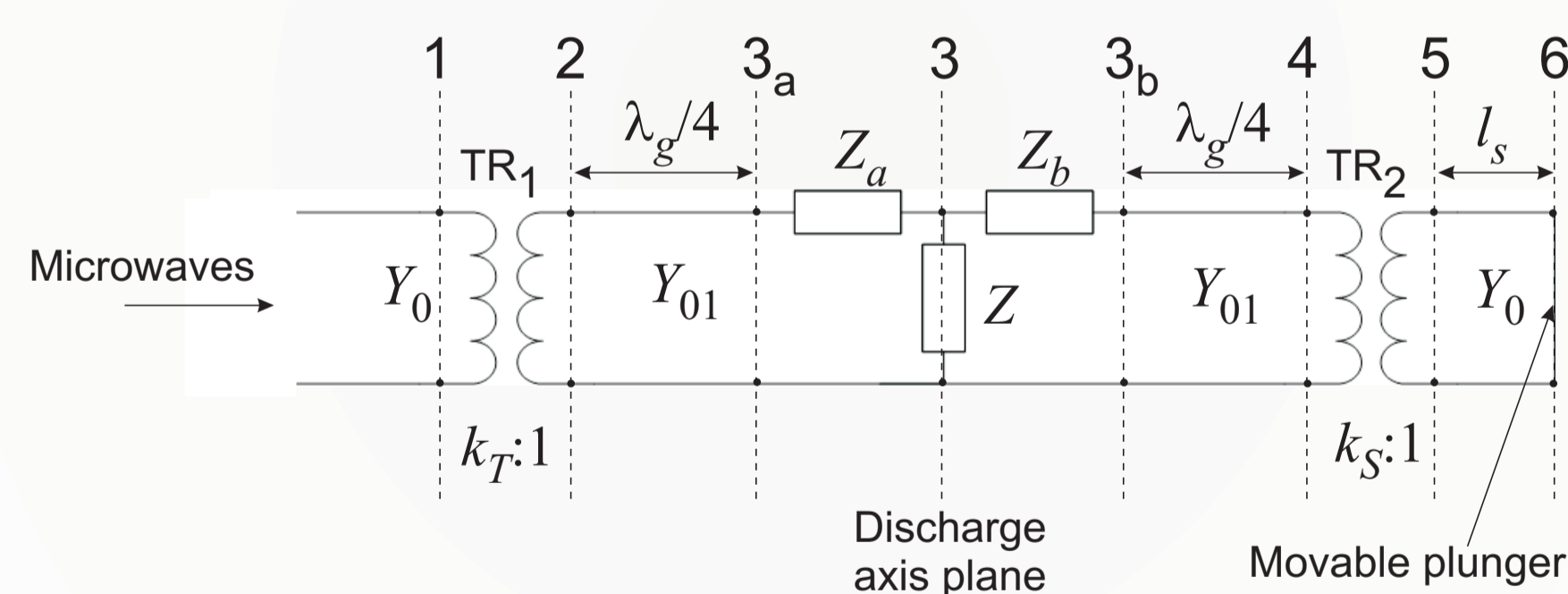
$$\frac{P_R}{P_I} \left( \frac{l_S}{\lambda_g} \right) = \left| \frac{y_{in} - 1}{y_{in} + 1} \right|^2$$

where  $P_I$  and  $P_R$  are the power of incident and reflected waves respectively,  $R_p$  and  $X_p$  are the plasma resistance and reactance respectively,  $Y_1$  is input admittance.

## MICROWAVE PLASMA SOURCE



Sketch of the MPS



Equivalent Circuit of the MPS

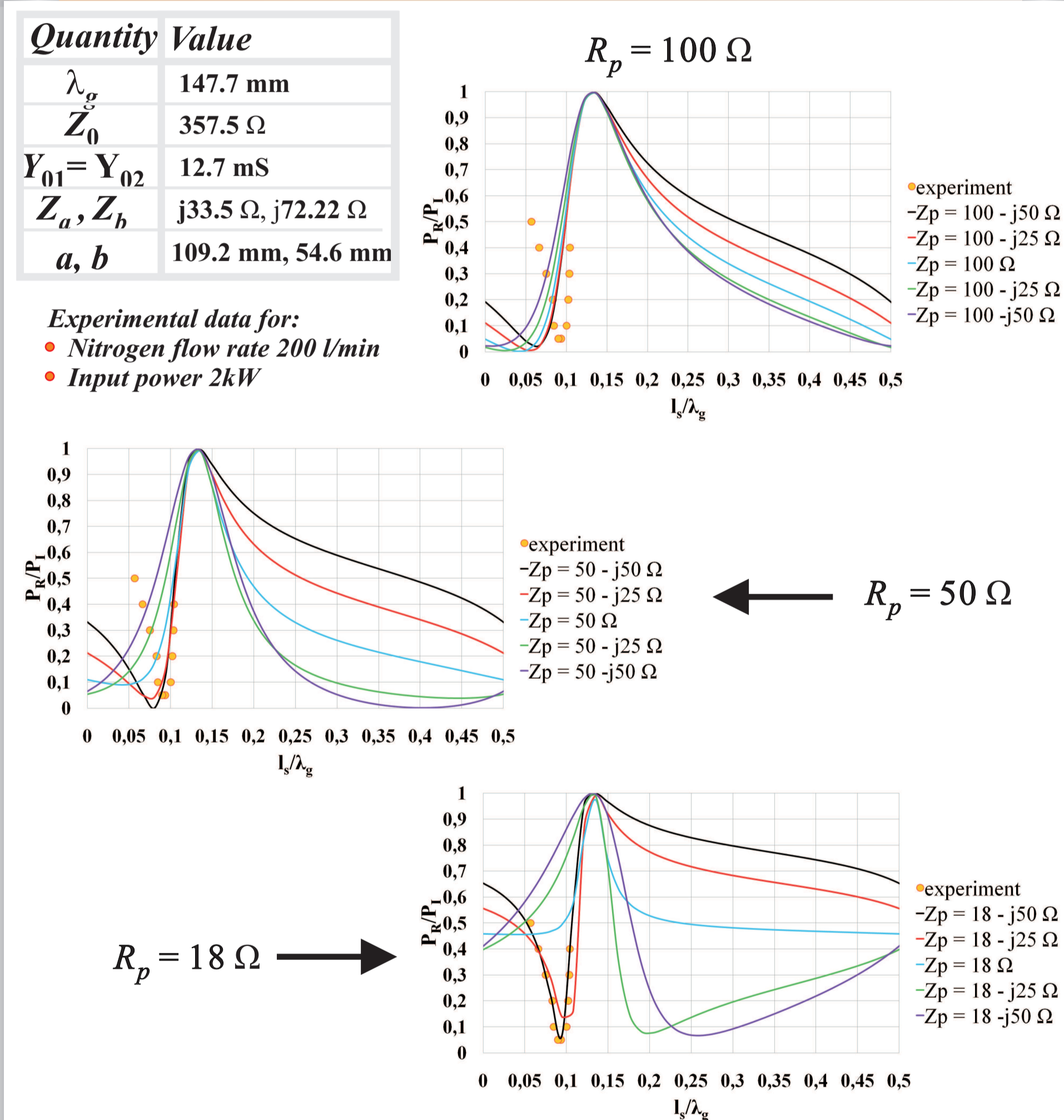
Quantity	Description
$\lambda_g$	Wave length in standard WR 430 waveguide
$l_S$	Movable plunger position
$Y_0 = 1/Z_0$	Characteristic admittance of standard WR 430 waveguide
$Z_0$	Characteristic impedance of standard WR 430 waveguide
$Y_{01} = Y_{02}$	Characteristic admittance of reduced height $b_1$ section
$\phi_{2IN}$	Inner diameter of brass cylinder
$Z_p$	Plasma impedance
$Z_a, Z_b$	Impedances representing discontinuity (holes) in reduced height waveguide
$k_T, k_S$	Transformation factors of the input and output transformer respectively
$a, b$	Standard WR 430 waveguide width and height respectively

## TUNING CHARACTERISTICS

Quantity Value

$\lambda_g$	147.7 mm
$Z_0$	357.5 $\Omega$
$Y_{01} = Y_{02}$	12.7 mS
$Z_a, Z_b$	j33.5 $\Omega$ , j72.22 $\Omega$
$a, b$	109.2 mm, 54.6 mm

Experimental data for:  
 • Nitrogen flow rate 200 l/min  
 • Input power 2kW



## CONCLUSIONS

- The calculated results and results achieved in experiment are very similar for assumed plasma resistance  $R_p = 18 \Omega$  and plasma reactance  $X_p = -50 \Omega$ .
- The power reflection coefficient  $P_R/P_I$  of the MPS is small (below 0.1) for narrow range of normalized movable plunger position